

The probability of a successful allocation of ball groups by boxes

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Abstract

Let $p = P_N^n$ be the probability of a successful allocation of n groups of distinguishable balls in N boxes in equiprobable scheme for group allocation of balls with the following assumption: each group contains m balls and each box contains not more than q balls from a same group. If $q = 1$, then we easily calculate p and observe that $p \rightarrow e^{-m(m-1)/2} \alpha_0$ as $n, N \rightarrow \infty$ such that $\alpha = n/N \rightarrow \alpha_0 < \infty$. In the case $2 \leq q$ we also find an explicit formula for the probability and prove that $p \rightarrow 1$ as $n, N \rightarrow \infty$ such that $\alpha = n/N \leq \alpha' < \infty$.

Keywords

Cauchy integral, Equiprobable scheme for group allocation of particles, Generating function